

# FitzGerald Relativity [DRAFT]

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# 1 Introduction

## 1.1 Scientific Theory

The ancients created myths populated with fantastic entities, extraordinary persons, and gods. These memorable stories created a language for describing why things are

as they are, and they guided expectation. This is what theories do, too. They create an idiom for discussion and prompt more or less useful expectation. These are respectively the normative, (prescriptive,) and the positive, (descriptive or predictive,) aspects of theory. Some theory, like music theory, is almost purely normative. Mathematical theories, like group theory, set theory, and graph theory, are purely normative. Newton's second law was normative in that it created a way to quantify force in terms of existing metrics for time, distance and mass. Most scientific theory is both normative and positive. Modern scientific theories are myths of today; they are stories that model reality in our thought but are never the reality itself.

## 1.2 Scientific Standards

Scientific theory is supposed to meet certain requirements: logical self-consistency, usefulness, testability. How do these criteria apply to normative and positive parts of a theory?

Intelligibility and logical self-consistency are required of the normative part of a theory. These are supported by a principle, Ockham's razor, associated with William of Ockham (c. 1287–1347), "Entities must not be multiplied beyond necessity," meaning the number of entities created or assumptions made is best kept to a minimum. Humorously stated, a theory should be as simple as possible but no simpler.

Testability, sometimes called falsifiability, pertains to the positive part of theory as clarified by Karl Popper (1902 – 1994), eminent philosopher of science.

1. It is easy to obtain confirmations, or verifications, for nearly every theory — if we look for confirmations.
2. Confirmations should count only if they are the result of risky predictions; that is to say, if, unenlightened by the theory in question, we should have expected an event which was incompatible with the theory — an event which would have refuted the theory.
3. Every "good" scientific theory is a prohibition: it forbids certain things to happen. The more a theory forbids, the better it is.
4. A theory which is not refutable by any conceivable event is non-scientific. Irrefutability is not a virtue of a theory (as people often think) but a vice.
5. Every genuine test of a theory is an attempt to falsify it, or to refute it. Testability is falsifiability; but there are degrees of testability: some theories are more testable, more exposed to refutation, than others; they take, as it were, greater risks.

6. Confirming evidence should not count except when it is the result of a genuine test of the theory; and this means that it can be presented as a serious but unsuccessful attempt to falsify the theory. (I now speak in such cases of "corroborating evidence.")
7. Some genuinely testable theories, when found to be false, are still upheld by their admirers — for example by introducing ad hoc some auxiliary assumption, or by reinterpreting the theory ad hoc in such a way that it escapes refutation. Such a procedure is always possible, but it rescues the theory from refutation only at the price of destroying, or at least lowering, its scientific status. (I later described such a rescuing operation as a "conventionalist twist" or a "conventionalist stratagem.")

One can sum up all this by saying that the criterion of the scientific status of a theory is its falsifiability, or refutability, or testability.<sup>1</sup>

Of course, no one considers refuting music theory.

The "conventionalist stratagem" to handle falsification is a not uncommon stop-gap when a satisfactory replacement theory has not yet been crafted.

Usefulness is realized from the conjunction of normative and positive parts. The normative aspect of a relativity theory must provide a consistent metrical framework for description, (positive part,) of events in the physical world, in particular, of the time and place of any event. It must provide a foundation for precise, lucid description of physical phenomena and of the physical laws and theories we construct to explain them. Its applicability must extend to any frame of reference.

Alternative theories may co-exist. A relativity theory must be judged first on whether it is self-consistent, then on whether its positive elements have withstood all tests, only then on usefulness or ease of use. A novel theory of relativity has an extra burden inasmuch as novelty compromises ease of use.

### 1.3 Scientific Revolution

What happens when a theory is falsified? This question was brilliantly answered by Thomas Kuhn in his book *The Structure of Scientific Revolutions*. The surprising answer, (with only slight hyperbole,) is, "nothing." Kuhn's study of historical cases reveals that normal science tends to be tightly focused on working within the

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<sup>1</sup> Karl Popper, *Conjectures and Refutations*, London: Routledge and Keagan Paul, 1963, pp. 33-39; from Theodore Schick, ed., *Readings in the Philosophy of Science*, Mountain View, CA: Mayfield Publishing Company, 2000, pp. 9-13.

prevailing paradigm. Evidence that a theory is false tends to be ignored, dismissed as flawed, dismissed as paradoxical, rationalized with a conventionalist twist and so forth. Most efforts are aimed at confirming the prevailing theory, evaluating parameters of the theory, and finding new applications of the theory. When a revolutionary new theory replaces an old theory it is largely the dying off of the old guard as a younger generation embraces the new theory. Perhaps, having a replacement theory ready to go when the old theory is discredited would facilitate a break from that unfortunate pattern.

Special relativity theory had vulnerabilities. The Lorentz transformation of event coordinates successively from frame to frame with non-parallel relative velocities produced absurd results when the last transformation closed a loop.<sup>2</sup> A corollary of special relativity, that one way speed of light is the same in every direction for every inertial frame, can be experimentally tested.<sup>3</sup> FitzGerald relativity is herein proposed to be the successor to Einstein's untenable special relativity theory.

## 1.4 Introduction to FitzGerald Relativity

It is well known that Heinrich Anton Lorentz acknowledged the priority of George Francis FitzGerald in suggesting the Michelson Morley experiment of 1887 might be explained by contraction of material bodies due to their velocity relative to the luminiferous ether. The transformation equations of Albert Einstein's special relativity (1905) are in consequence sometimes called the Lorentz-FitzGerald transformations. Yet, these three held different concepts.

FitzGerald conjectured in 1889:

...that almost the only hypothesis that can reconcile this ... is that the length of material bodies changes, according as they are moving through the ether or across it, by an amount depending on the square of the ratio of their velocity to that of light. We know that electric forces are affected by the motion of the electrified bodies relative to the ether, and it seems a not improbable supposition that the molecular forces are affected by the motion, and that the size of a body alters consequently.<sup>4</sup>

This remarkable conjecture anticipated recognition that chemical bonds are electromagnetic in nature and suggested that length contraction consequently occurs across

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<sup>2</sup>Wallace, D. B., "Refutation of Lorentz-Einstein Special Relativity" academia.edu, 26 December 2016

<sup>3</sup>Wallace, D. B., "A Revealing Test of the Compatibility of Special Relativity Postulates"

<sup>4</sup>FitzGerald, G. F., "The Ether and the Earth's Atmosphere," Science v. XIII No. 328, p. 390, 1889

as well as along the direction of motion. It thus uniquely offers a physical explanation of Michelson's and Morley's null result.

The electromagnetic field is not a material substance, but its reality is evident. According to Maxwell's theory of electromagnetism, disturbances in the electromagnetic field are propagated isotropically at a constant speed  $c$  in free space. The medium of this propagation is the field itself, not some ethereal substance. Speculation about a dragged or deformed luminiferous ether was triggered by the surprising outcome of the Michelson Morley experiment. Michelson expected that the round trip of light between two points on a stone slab of presumed stable dimensions, would take longer if the stone slab were moving relative to the ether, by the factor  $1/(1 - v^2/c^2)$  if the points were aligned parallel to their velocity  $\vec{v}$ , and by  $1/\sqrt{1 - v^2/c^2}$  if aligned perpendicular to the velocity. However, he observed no discernable difference.

The purport of FitzGerald's conjecture was that the two points were not a fixed distance apart as Michelson had supposed; rather, that the forces holding a material body together were electromagnetic, (a novel idea in itself,) and governed the material dimensions of the stone slab causing contraction by the factor  $1 - v^2/c^2$  along the direction of motion and by  $\sqrt{1 - v^2/c^2}$  perpendicular to it; thus cancelling the expected change in round trip time.

In their attempts to account for the Michelson Morley null result, both Lorentz and FitzGerald related the length contraction of their conjectures to velocity relative to an absolute frame of reference, the luminiferous ether, characterized by isotropy of one way light speed. Lorentz, unlike Einstein, was not committed to zero transverse contraction, but noted that any deformation related to velocity must have a longitudinal to transverse ratio of  $\sqrt{1 - v^2/c^2}$ .

Einstein rejected the notion of a luminiferous ether. He declared "absolute rest" meaningless and considered velocity to be strictly relative. Einstein, by his own testimony, was unfamiliar with the Michelson Morley experiment when he wrote his special relativity paper. He envisioned trying to measure the speed of light using clocks, though clocks of that day were nowhere near stable and accurate enough for the purpose. His special relativity was a speculation without supporting experimental evidence.

FitzGerald died in 1901, prior to the advent of special relativity. He did not include equations in his brief conjecture. From his words, however, a different set of transformation equations is easily constructed. From these FitzGerald equations an entirely new theory of relativity unfolds, no less empirically successful, more intuitive, free of ambiguities and paradoxes and incorporating the notion of absolute rest. Detailed description of this FitzGerald relativity is the subject of this paper.

## 2 FitzGerald Coordinate Transformations

### 2.1 Events and Space-Time Coordinates

In keeping with the instincts of FitzGerald and Lorentz, only one inertial frame of reference, called the rest frame, will be deemed absolutely stationary so that light speed is isotropic, i. e. the same in every direction. Throughout this paper, reference will be made to local frames of reference, each being fully specified by its origin and its constant velocity relative to the rest frame. The absolute velocity of a local frame will usually be given as the ratio of its velocity to the speed of light,  $\vec{\beta} = \frac{\vec{v}}{c}$ . Local frames differing in choice of origin still demarcate the same inertial frame if the coordinate origins have the same velocity relative to the rest frame.

Time is understood to be one thing, not a different thing in each frame of reference. All clocks are to be synchronized in the rest frame. The use of local time synchronization, based on the assumption that light signals between the local origin and the clock take the same time in each direction, is deprecated as a fiction in all but the rest frame where it is strictly true; however, the likelihood that the practice will continue compels inclusion of a transformation between local time and rest frame time. Current international time standards are synchronized in the earth center inertial frame because earth rotation puts clocks around the world in different inertial frames; they could as well use the rest frame.

Discussions of light and time will be idealized with light speed always  $c$  relative to the rest frame, and clock rate the same for all clocks regardless of motion or position.

As a point has three spatial coordinates,  $(x, y, z)$ , an event has four coordinates,  $(x, y, z, t)$ , three of space and one of time. The spatial coordinate values are frame of reference specific because spatial coordinates will be in local length units. The coordinates of an event  $E$  are usually given as absolute ( $E_0$  relative to the rest frame,) or local ( $E_\beta$  local length with rest frame time,) but may for special purposes be either fully local including local time ( $E_{\beta, \text{local}}$ ) or rest frame metrics relative to a local origin ( $E_{\beta, 0}$  subscript order being frame-of-reference, metric.)

### 2.2 Required Alignment of Coordinates

Lorentz equations of special relativity and FitzGerald equations both transform space-time coordinates of an event relative to one inertial coordinate system into the space-time coordinates of the same event relative to another. Both require the x-axes of the two systems to coincide and the other axes to be parallel. Only the FitzGerald equations also require that one frame be the rest frame and that the other

frame use rest frame time rather than local time. “Rest frame” is deemed meaningless in special relativity. Both Lorentz and FitzGerald equations require the origins to coincide at time zero; this puts a constraint on origin choice for Lorentz equations,<sup>5</sup> but not for FitzGerald equations.

In special relativity, the velocity variable of the Lorentz equations is the velocity of one inertial frame relative to another. The length contraction and time dilation are held to be virtual and frame of reference dependent. The same equations serve as the inverse transformation. Thus special relativity denies the uniqueness of the rest frame. The normative definitions included in special relativity preclude identification of an absolute rest frame.

The velocity variable  $v_0$  of the FitzGerald equations is velocity in the positive x-direction relative to absolute rest; in FitzGerald relativity it is possible to deduce absolute velocity from empirical tests, (see section 9.) Length contraction is understood to be actual contraction of condensed matter. The contraction of moving solid length standards produces a virtual lengthening of spatial distance as compared to rest frame measure. All frames share rest frame time so there is no time dilation.<sup>6</sup> The reverse transformation is distinct from the forward transformation.<sup>7</sup> The frame of reference of a variable will be indicated by a subscript, usually the frame’s velocity as a fraction of light speed, e. g.  $\phi_\beta$ , with a subscript zero for the absolute rest frame, e. g.  $\phi_0$ .

## 2.3 Equation Summary

The name of a vector will represent the magnitude of the vector unless clearly shown as a vector, e. g.  $\vec{\beta}$ .

Here for comparison are the equations.

Lorentz Equations

$$\beta \equiv \frac{v}{c}$$

$$\gamma \equiv \frac{1}{\sqrt{1-\beta^2}}$$

FitzGerald Equations

$$\beta \equiv \frac{v_0}{c}$$

$$\gamma \equiv \frac{1}{\sqrt{1-\beta^2}}$$

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<sup>5</sup>When local time is used, the local origin must be a point where local time coincides with rest frame time.

<sup>6</sup>Clock rate changes are not conflated with time rate changes.

<sup>7</sup>Rest frame is considered un-transformed, so “forward” is from rest frame to moving frame, and “reverse” restores rest frame.



	Forward		Reverse	
$t_B = \gamma \left( t_A - \frac{vx_A}{c^2} \right)$	$t = t$		$t = t$	
$x_B = \gamma(x_A - vt_A)$	$x_\beta = \gamma^2(x_0 - \beta ct)$	(15)	$x_0 = \frac{x_\beta}{\gamma^2} + \beta ct$	(18)
$y_B = y_A$	$y_\beta = \gamma y_0$	(16)	$y_0 = \frac{y_\beta}{\gamma}$	(19)
$z_B = z_A$	$z_\beta = \gamma z_0$	(17)	$z_0 = \frac{z_\beta}{\gamma}$	(20)
Local time:	$t_\beta = \gamma^2 \left( t_0 - \frac{\beta x_0}{c} \right)$	(22)	$t_0 = t_\beta + \frac{\beta x_\beta}{c}$	(23)
Good to know:	$\gamma^2 \beta^2 = \gamma^2 - 1$		$0 \leq \beta < 1 \leq \gamma$	
Trig Functions	$\tan \phi_\beta = \frac{\tan \phi_0}{\gamma}$	(24)	$\tan \phi_0 = \gamma \tan \phi_\beta$	(25)
of Angle	$\sin \phi_\beta = \frac{\sin \phi_0}{\gamma \sqrt{1 - \beta^2 \sin^2 \phi_0}}$	(26)	$\sin \phi_0 = \frac{\sin \phi_\beta}{\sqrt{1 - \beta^2 + \beta^2 \sin^2 \phi_\beta}}$	(27)
from $\vec{\beta}$	$\cos \phi_\beta = \frac{\cos \phi_0}{\sqrt{1 - \beta^2 + \beta^2 \cos^2 \phi_0}}$	(28)	$\cos \phi_0 = \frac{\cos \phi_\beta}{\gamma \sqrt{1 - \beta^2 \cos^2 \phi_\beta}}$	(29)

The alert reader will have noticed that, for local time and for spatial coordinates, the right sides of the Lorentz equations, if multiplied by  $\gamma$ , yield the right sides of the forward FitzGerald equations, and for all but the  $x$  coordinate, if divided by  $\gamma$ , yield the right sides of the reverse FitzGerald equations. The use of rest frame time rather than local time is responsible for the  $x$  coordinate exception.

## 2.4 Transformation Matrices

Transformation of position vectors can be effected with matrix operators.

$$\mathbf{F}\mathbf{p}_0 - \gamma^2\mathbf{q} = \mathbf{p}_\beta \quad (1)$$

$$\mathbf{G}\mathbf{p}_\beta + \mathbf{q} = \mathbf{p}_0 \quad (2)$$

where

$$\mathbf{p}_0 = \begin{pmatrix} x_0 \\ y_0 \\ z_0 \end{pmatrix} \quad (3)$$

$$\mathbf{q} = \begin{pmatrix} \beta ct \\ 0 \\ 0 \end{pmatrix} \quad (4)$$

$$\mathbf{p}_\beta = \begin{pmatrix} x_\beta \\ y_\beta \\ z_\beta \end{pmatrix} \quad (5)$$

$$\mathbf{F} = \begin{pmatrix} \gamma^2 & 0 & 0 \\ 0 & \gamma & 0 \\ 0 & 0 & \gamma \end{pmatrix} \quad (6)$$

$$\mathbf{G} = \begin{pmatrix} \frac{1}{\gamma^2} & 0 & 0 \\ 0 & \frac{1}{\gamma} & 0 \\ 0 & 0 & \frac{1}{\gamma} \end{pmatrix} \quad (7)$$

## 2.5 Equation Derivations

### 2.5.1 A Round Trip of Light

To begin our derivation of the relation of frame dependent quantities, see figure 1, representing the round trip of a light signal from point  $P$  to  $Q$  and back, as they move at constant velocity  $v_0 = \beta c$  relative to the rest frame. Although  $P$  and  $Q$  are moving in the rest frame, they are fixed relative to each other.

We take  $A$  and  $P$  as the origins of stationary and moving frames, respectively, coinciding at  $t = 0$ . We let the x-axis be parallel to the velocity. We let the z-coordinate go unexpressed as it is zero throughout.

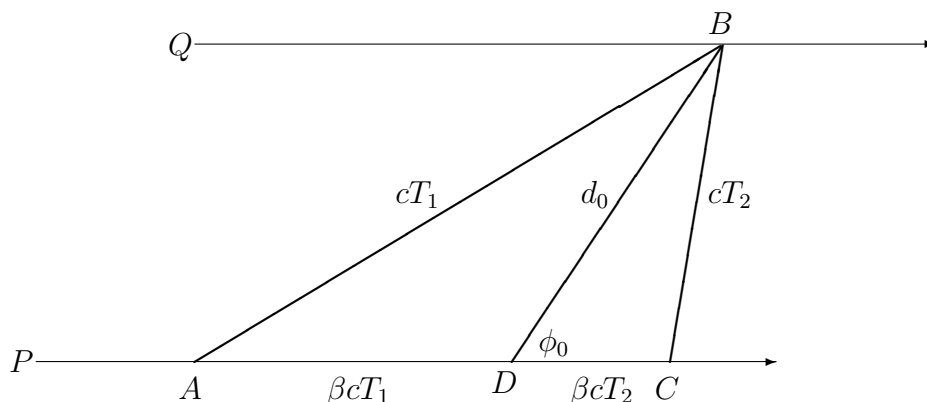
The rest frame time scale is used everywhere, as if clocks have been synchronized using light or radio signals understood to have velocity  $c$  relative to the rest frame.

The light signal, to begin its round trip, originates from  $P$  when  $P$  is at point  $A$ , our space-time origin. The light signal reaches  $Q$  at time  $t = T_1$  when  $Q$  and  $P$  are at points  $B$  and  $D$  respectively. The signal, being reflected at  $B$ , returns to  $P$  at  $t = T_1 + T_2$  when  $P$  is at point  $C$ . The points  $A$ ,  $B$ ,  $C$ , and  $D$  are fixed points in the rest frame marking the locations of these events. Light path lengths are: from  $A$  to  $B$ ,  $cT_1$ , and from  $B$  to  $C$ ,  $cT_2$ .

The rest frame measure of angle  $\angle CDB$  between the velocity  $\vec{v}_0 = \vec{\beta}c$  and the direction  $P$  to  $Q$  is  $\phi_0$ . The rest frame distance between points  $P$  and  $Q$ , (same as the distance between  $D$  and  $B$ ), is  $d_0$ . Path lengths for the moving point  $P$  are from  $A$  to  $D$ ,  $\beta cT_1$ , and from  $D$  to  $C$ ,  $\beta cT_2$ . All times, distances and angles are relative to the rest frame.

We explore the relationship of these quantities in pursuing our ultimate purpose to derive the moving frame distance  $d_\beta$ .

Figure 1



The cosine law and quadratic formula yield solutions in variables  $d_0$ ,  $\beta c$ , and  $\phi_0$  for  $T_1$  and  $T_2$  in the triangles  $\triangle ADB$  and  $\triangle CDB$  respectively. First, we find  $T_1$  of triangle  $\triangle ADB$  in equations (8) through (10) using the law of cosines.

$$c^2T_1^2 = \beta^2c^2T_1^2 + d_0^2 + 2\beta cT_1d_0 \cos \phi_0 \quad (8)$$

We write (8) in standard quadratic form.

$$(1 - \beta^2)c^2T_1^2 - 2\beta cd_0 \cos \phi_0 T_1 - d_0^2 = 0 \quad (9)$$

We solve for  $T_1$  using the quadratic formula.

$$T_1 = \frac{d_0 \left( \beta \cos \phi_0 + \sqrt{1 - \beta^2 \sin^2 \phi_0} \right)}{c(1 - \beta^2)} \quad (10)$$

Now, we find  $T_2$  of triangle  $\triangle CDB$  in equations (11) through (13).

$$c^2T_2^2 = \beta^2c^2T_2^2 + d_0^2 - 2\beta cT_2d_0 \cos \phi_0 \quad (11)$$

We write (11) in standard quadratic form.

$$(1 - \beta^2)c^2T_2^2 + 2\beta cd_0 \cos \phi_0 T_2 - d_0^2 = 0 \quad (12)$$

We solve for  $T_2$  using the quadratic formula.

$$T_2 = \frac{d_0 \left( -\beta \cos \phi_0 + \sqrt{1 - \beta^2 \sin^2 \phi_0} \right)}{c(1 - \beta^2)} \quad (13)$$

### 2.5.2 Moving Length

In the proper frame of  $P$  and  $Q$ , the distance from  $P$  to  $Q$  is judged by the round trip time of the light signal,  $d_\beta = \frac{c(T_1+T_2)}{2}$ .

$$d_\beta = \frac{c}{2} \left( \frac{d_0 \left( \beta \cos \phi_0 + \sqrt{1 - \beta^2 \sin^2 \phi_0} \right)}{c(1 - \beta^2)} + \frac{d_0 \left( -\beta \cos \phi_0 + \sqrt{1 - \beta^2 \sin^2 \phi_0} \right)}{c(1 - \beta^2)} \right)$$

which simplifies to

$$d_\beta = \gamma^2 d_0 \sqrt{1 - \beta^2 \sin^2 \phi_0} \quad (14)$$

The spatial distance appears greater in the moving frame because the local measuring sticks are contracted.

### 2.5.3 Spatial Coordinate Conversion

The rest frame coordinates of  $Q$  are  $(\beta ct + d_0 \cos \phi_0, d_0 \sin \phi_0)$ . For length parallel to the velocity, the special case  $\phi_0 = 0$ , our moving length equation yields the forward transformation of the x-coordinate.

$$x_\beta = \gamma^2(x_0 - \beta ct) \quad (15)$$

Take note that when transforming the difference of x-coordinates at a fixed time, the  $\beta ct$  terms cancel, so  $\Delta x_\beta = \gamma^2 \Delta x_0$ .

For the perpendicular case,  $\phi_0 = \frac{\pi}{2}$ , we have our forward transformation of the y-coordinate.

$$y_\beta = \gamma y_0 \quad (16)$$

By symmetry, the forward transformation of the z-coordinate is

$$z_\beta = \gamma z_0 \quad (17)$$

Now we can solve the equations (15) through (17) to find the reverse transformations.

$$x_0 = \frac{x_\beta}{\gamma^2} + \beta ct \quad (18)$$

$$y_0 = \frac{y_\beta}{\gamma} \quad (19)$$

$$z_0 = \frac{z_\beta}{\gamma} \quad (20)$$

#### 2.5.4 Reverse Length Conversion

$$\begin{aligned} d_0 &= \sqrt{x_0^2 + y_0^2 + z_0^2} \\ &= \sqrt{\frac{x_\beta^2}{\gamma^4} + \frac{y_\beta^2 + z_\beta^2}{\gamma^2}} \\ &= \sqrt{\frac{d_\beta^2 \cos^2 \phi_\beta}{\gamma^4} + \frac{d_\beta^2 \sin^2 \phi_\beta}{\gamma^2}} \\ &= \frac{d_\beta}{\gamma} \sqrt{(1 - \beta^2) \cos^2 \phi_\beta + \sin^2 \phi_\beta} \\ d_0 &= \frac{d_\beta}{\gamma} \sqrt{1 - \beta^2 \cos^2 \phi_\beta} \end{aligned} \quad (21)$$

#### 2.5.5 Local Time

FitzGerald relativity is normative in the matter of time. It does not make claims about the physics of clocks; rather, it prescribes what clocks should do. One time scale for all frames is fundamental to FitzGerald relativity.

We now consider the deprecated use of local time and how it relates to the standard rest frame time of FitzGerald relativity. We must heed the requirement, familiar in special relativity, that the origins of the two frames be coincident and synchronized at time zero. The synchronizations are coordinate dependent, but the length of the time unit is to be the same in all frames so the moving origin will remain synchronized with the rest frame.

Referring again to figure 1, the reflection at  $B$  occurs at  $t_0 = T_1$ , but in the frame

of  $P$  and  $Q$  local time of the reflection is taken to be  $t_\beta = \frac{T_1+T_2}{2}$ .

$$\begin{aligned}
t_\beta - t_0 &= \frac{T_1 + T_2}{2} - T_1 \\
&= \frac{T_2 - T_1}{2} \\
&= \frac{\left( \frac{d_0(-\beta \cos \phi_0 + \sqrt{1-\beta^2 \sin^2 \phi_0})}{c(1-\beta^2)} \right) - \left( \frac{d_0(\beta \cos \phi_0 + \sqrt{1-\beta^2 \sin^2 \phi_0})}{c(1-\beta^2)} \right)}{2} \\
&= \frac{-d_0 \beta \cos \phi_0}{c(1-\beta^2)}
\end{aligned}$$

For any choice of  $d_0$  and  $\phi_0$  this becomes,

$$\begin{aligned}
t_\beta - t_0 &= \frac{-\beta \gamma^2 (x_0 - \beta c t_0)}{c} \\
t_\beta &= \gamma^2 \left( t_0 - \frac{\beta x_0}{c} \right) \tag{22}
\end{aligned}$$

At the origin of the moving frame with  $x_0 = \beta c t_0$  this reduces to  $t_\beta = t_0$ , as required.

The reverse transformation is

$$t_0 = \frac{t_\beta}{\gamma^2} + \frac{\beta x_0}{c}$$

Substituting for  $x_0$ ,

$$t_0 = \frac{t_\beta}{\gamma^2} + \frac{\beta \left( \frac{x_\beta}{\gamma^2} + \beta c t_0 \right)}{c}$$

Re-solving for  $t_0$ ,

$$t_0 = t_\beta + \frac{\beta x_\beta}{c} \tag{23}$$

These time transformations differ from the Lorentz time transformations by the factor  $\gamma$ .

### 2.5.6 Angle Measure

By applying coordinate conversion to the trigonometric functions of  $\phi$ , a stable<sup>8</sup> angle with one ray parallel to the x-axis, we learn the relation of rest and moving frame measure of angles.

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<sup>8</sup>Stable means the relative positions of the rays determining the angle do not change with time or are taken at the same specified rest frame time.

Tangent forward,

$$\tan \phi_\beta = \frac{\Delta y_\beta}{\Delta x_\beta} = \frac{\tan \phi_0}{\gamma} \quad (24)$$

and reverse,

$$\tan \phi_0 = \gamma \tan \phi_\beta \quad (25)$$

Sine forward,

$$\begin{aligned} \sin \phi_\beta &= \frac{\Delta y_\beta}{\Delta d_\beta} = \frac{\gamma \Delta y_0}{\gamma^2 \Delta d_0 \sqrt{1 - \beta^2 \sin^2 \phi_0}} \\ \sin \phi_\beta &= \frac{\sin \phi_0}{\gamma \sqrt{1 - \beta^2 \sin^2 \phi_0}} \end{aligned} \quad (26)$$

and reverse,

$$\sin \phi_0 = \frac{y_0}{d_0} = \frac{\sin \phi_\beta}{\sqrt{1 - \beta^2 \cos^2 \phi_\beta}}$$

or written with sine only

$$\sin \phi_0 = \frac{\sin \phi_\beta}{\sqrt{1 - \beta^2 + \beta^2 \sin^2 \phi_\beta}} \quad (27)$$

Cosine forward,

$$\begin{aligned} \cos \phi_\beta &= \frac{\Delta x_\beta}{\Delta d_\beta} = \frac{\gamma^2 \Delta x_0}{\gamma^2 \Delta d_0 \sqrt{1 - \beta^2 \sin^2 \phi_0}} \\ \cos \phi_\beta &= \frac{\cos \phi_0}{\sqrt{1 - \beta^2 \sin^2 \phi_0}} \end{aligned}$$

or written with cosine only

$$\cos \phi_\beta = \frac{\cos \phi_0}{\sqrt{1 - \beta^2 + \beta^2 \cos^2 \phi_0}} \quad (28)$$

and reverse,

$$\cos \phi_0 = \frac{\Delta x_0}{d_0} = \frac{\cos \phi_\beta}{\gamma \sqrt{1 - \beta^2 \cos^2 \phi_\beta}} \quad (29)$$

For angles  $\psi$  with both rays perpendicular to the x-axis the relationship is an identity,  $\psi_\beta = \psi_0$ .

Any angle with rays  $\vec{j}$  and  $\vec{k}$  co-planar with the x-axis equals the difference of the two angles formed with the x-axis by rays  $\vec{j}$  and  $\vec{k}$  respectively.

For any other angle with rays  $\vec{j}$  and  $\vec{k}$ , conversion is possible either by transforming points and recomputing angles or by employing spherical trigonometry with the angle  $\psi$  between the two planes containing angles  $\phi$  made by  $\vec{j}$  and  $\vec{k}$ , respectively, with the x-axis.

Angles determined by non-simultaneous events, in contrast to stable angles determined by relatively fixed points, are especially frame dependent. Angles determined in a different frame by the same non-simultaneous events may be found by transformation of the determining events and applying the cosine law. In figure 1, for example, the angle with the x-axis of the light path from emission to reflection is  $\angle CAB$  in the rest frame and  $\angle CDB$  in the proper frame of  $P$  and  $Q$ .

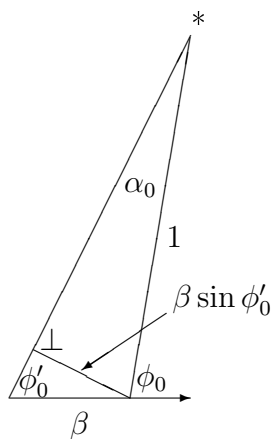
### 3 Elementary Applications (work in progress)

#### 3.1 Radar

Radar measures distance in the frame of the radar site,  $d = \frac{T}{2c}$ , by timing radio pulses from transmission to reception of the reflected pulse. If the target being tracked is moving relative to the site, the distance at the time of pulse reflection is being measured. Because rest frame time of the reflection event is not revealed,

it is customary to use the local time half-way between transmission and reception. If direction to the reflection and  $\vec{\beta}$  for the radar site are known, the rest frame time of the reflection can be calculated using the reverse local time transformation, equation (23).

$$t_0 = t_\beta + \frac{\beta \cos \phi_\beta}{c} \quad (30)$$



Stellar Aberration  
Figure 3

To find rest frame coordinates of the reflector, convert its site centered moving frame coordinates to rest frame measure and add to the rest frame coordinates of the radar site at the rest frame time of reflection.

For radar operating in or through the atmosphere some correction for refraction may be appropriate.

#### 3.2 Stellar Aberration

An observer's motion causes stellar aberration, an angular shift  $\alpha$  of a star's apparent position in the direction of  $\vec{\beta}$  from its true position. As light from the star travels



one unit distance, the observer moves  $\beta$  unit distance. The triangle in figure three shows the rest frame measure of the apparent angle of the star to be  $\phi'_0 = \phi_0 - \alpha_0$ .

$$\phi'_0 = \phi_0 - \alpha_0 \quad (31)$$

$$\sin(\alpha_0) = \beta \sin(\phi'_0) \quad (32)$$

$$\sin(A + B) = \sin A \cos B + \cos A \sin B \quad (\text{trigonometric identity})$$

$$\sin \phi_0 = \sin \phi'_0 \cos \alpha_0 + \cos \phi'_0 \sin \alpha_0 \quad (33)$$

Defining  $\alpha_\beta$  relative to  $\phi_0$ ,

$$\alpha_\beta = \phi_0 - \phi'_\beta \quad (34)$$

$$\alpha_\beta = \arcsin \left( \frac{\sin \phi'_\beta}{\sqrt{1 - \beta^2 \cos^2 \phi'_\beta}} \right) + \arcsin \left( \frac{\beta \sin \phi'_\beta}{\sqrt{1 - \beta^2 \cos^2 \phi'_\beta}} \right) - \phi'_\beta \quad (35)$$

Using the cosine law

$$1^2 = \beta^2 + k^2 - 2\beta k \cos(\phi_0 - \alpha_0) \quad (36)$$

$$\cos(\phi_0 - \alpha_0) = \frac{\beta^2 + k^2 - 1}{2\beta k} \quad (37)$$

$$k^2 = \beta^2 + 1^2 + 2\beta \cos \phi_0 \quad (38)$$

Combine these,

$$\cos(\phi_0 - \alpha_0) = \frac{\beta^2 + \beta^2 + 1^2 + 2\beta \cos \phi_0 - 1}{2\beta \sqrt{\beta^2 + 1^2 + 2\beta \cos \phi_0}} \quad (39)$$

then simplify.

$$\cos(\phi_0 - \alpha_0) = \frac{\beta + \cos \phi_0}{\sqrt{\beta^2 + 2\beta \cos \phi_0 + 1}} \quad (40)$$

Transform the cosine to the observer's frame value,

$$\cos(\phi_\beta - \alpha_\beta) = \frac{\cos(\phi_0 - \alpha_0)}{\sqrt{1 - \beta^2 + \beta^2 \cos^2(\phi_0 - \alpha_0)}} \quad (41)$$

Use equation (40) to substitute for  $\cos(\phi_0 - \alpha_0)$  in equation (41),

$$\cos(\phi_\beta - \alpha_\beta) = \frac{\frac{\beta + \cos \phi_0}{\sqrt{\beta^2 + 2\beta \cos \phi_0 + 1}}}{\sqrt{1 - \beta^2 + \beta^2 \left( \frac{\beta + \cos \phi_0}{\sqrt{\beta^2 + 2\beta \cos \phi_0 + 1}} \right)^2}} \quad (42)$$

and simplify.

$$\cos(\phi_\beta - \alpha_\beta) = \frac{\beta + \cos \phi_0}{1 + \beta \cos(\phi_0)} \quad (43)$$

Therefore,

$$\alpha_\beta = \arccos \frac{\cos \phi_0}{\sqrt{1 - \beta^2 + \beta^2 \cos^2 \phi_0}} - \arccos \frac{\beta + \cos \phi_0}{1 + \beta \cos(\phi_0)} \quad (44)$$

We want  $\phi_0$  as a function of  $\beta$  and  $\phi_\beta - \alpha_\beta$ . So, we solve equation (43) for  $\phi_0$ .

$$\phi_0 = \arccos \frac{\cos(\phi_\beta - \alpha_\beta) - \beta}{1 - \beta \cos(\phi_\beta - \alpha_\beta)} \quad (45)$$

**Reminder:** The equation for transforming  $\phi$  is not to be used to transform  $\alpha$  directly.

### 3.3 Small Angle Transformation

Small differences in angle from  $\vec{\beta}$  can be transformed to a good approximation using the derivative

$$\Delta \phi_\beta = \Delta \phi_0 \left( \frac{1 + \tan^2 \phi_0}{\gamma \left( 1 + \frac{\tan^2 \phi_0}{\gamma^2} \right)} \right) \quad (46)$$

$$\Delta \phi_0 = \Delta \phi_\beta \left( \frac{\gamma (1 + \tan^2 \phi_\beta)}{1 + \gamma^2 \tan^2 \phi_\beta} \right) \quad (47)$$

### 3.4 Loop and Polygonal Light Paths

If we can envision a light signal as a moving point, we can envision a light path as the set of fixed points the signal has traversed. A point of the path is the same for multiple frames of reference only at the moment when the signal is at the point.

Our standard of length is defined in terms of time taken by a round trip of light. Consequently, the unit of length contracts as velocity increases. That is, the length unit is dependent on  $\beta$  of the frame of reference, and also on orientation. A light signal that follows a polygon of perimeter  $P_\beta$  by reflections at each vertex completes the cycle in either direction in a time interval  $T = \frac{P_\beta}{c}$  whether the polygon is at rest or moving. The perimeter measure by an un-contracted measuring stick will be less for a non-rotating, inertially moving polygonal figure in the same ratio as for length perpendicular to  $\beta$ .

$$P_\beta = P_0 \sqrt{1 - \beta^2} \quad (48)$$

The light path, however, is an open polygonal line in any frame other than the proper frame of the polygon. Length in each frame being defined in terms of light speed, and time being the same in every frame, it might seem that the light path length must be the same in every frame. It is not, however, because the round trip in the proper frame is not a round trip in other frames. If in other than the proper frame light were to retrace its path to make a round trip, the times for the two directions would not in general be equal, and the retraced path would be closed not in the frame of the polygon but in the frame having the opposite  $\beta$ .

### 3.5 The Sagnac Effect

The Sagnac effect pertains to light following a plane polygon that rotates in its plane. In this case, the time light takes depends on the area enclosed, the rotation rate, and whether the light direction is the same or counter to the rotation.

In the proper frame of the center of rotation, the vertex of origin moves before the signal returns; the light path is not closed. If the light closes the path by a final reflection to the place of origin, it will have followed a path that is the same length in every frame. The length of the last segment

### 3.6 Empirical Determination of Beta

In 1905, special relativity was founded on the notion that synchronization of clocks remote from one another was impossible except in the sense of local synchronization that assumes isotropy of light speed in the local frame. That was before the invention of atomic clocks. Now we can do better.

We understand that even atomic clock rates are subject to influences. Our understanding of these influences allows us to compensate for them. Absolute velocity is supposed to be one such influence, so after an initial estimate may need successive determinations to improve accuracy.

If we synchronize two clocks, perhaps while they are together, and if we neutralize the rate disturbances, the clocks would continue to be synchronized as they move apart.

With atomic clocks in orbiting satellites, as we have in the GPS system, the clocks cannot be placed in proximity for synchronization, yet they are synchronized based on observations over many times and relative positions. In practice, GPS clocks are synchronized to local time of the earth centered inertial frame by a complex statistical process. A different, but similarly complex process could synchronize them to rest frame time.

GPS satellites are in nearly circular orbits with orbital periods about twelve hours. If the time encoded transmissions of each satellite could be received and echoed by the other satellites, we would have all the data we need to make a high precision determination of  $\beta$ .

Take two satellites,  $A$  and  $B$ . If  $A$  transmits a signal at  $t_1$ , to be echoed by  $B$  at  $t_2$ , and received at  $A$  at  $t_3$  then, in the inertial frame with origin at  $A$  for the transmission and reception events, the distance to the echo event at  $B$  is  $\frac{t_3-t_1}{2c}$ , but the relation of clock times is as yet undetermined.

We could time a light signal in each direction between the synchronized clocks.

The relative speed of light between them will depend on  $\vec{\beta}$ :

$$c_{rel} = \beta \tag{49}$$

and by timing light signals one could determine  $\vec{\beta}$ .

In the GPS system we have several atomic clocks moving relative to 3.3 If we have due to motion relative to the rest frame. If the orientation of the pair is perpendicular to  $\vec{\beta}$  the times will be equal; if parallel to  $\vec{\beta}$  the difference will be  $T_1 - T_2 =$  varying both distance and direction relative to each other, and if these clocks communicate time encoded in light signals so light travel time between them in each direction could be observed, then the orientation and magnitude of  $\beta$  would be readily apparent.

We shall idealize a pair of like atomic clocks in orbit about each other. As the clocks orbit they use light signals to communicate time for comparison. We shall develop an algorithm to find  $\vec{\beta}$ , the influence of  $\vec{\beta}$  on clock rate, and the influence of gravitational potential on clock rate from the relation between clock difference and orientation in space. We assume there is no other source of clock rate variation.

### 3.6.1 Special Case # 1: Zero Barycenter Velocity and Invariant Gravitational Potential

If our clocks are in circular orbit about each other in deep space where there is no variation of gravitational potential, and their barycenter is at absolute rest, then the clocks maintain an unvarying difference. Gravitational potential and the magnitude of the velocity are, in this case, constant.

Because the orbit is circular and at rest, the light signals take the same time in each direction. If signal time in one direction is  $T_1$  and in the other direction  $T_2$ , then the distance between the clocks is  $\frac{T_1+T_2}{2c}$ . The signal distance difference is  $\frac{T_1-T_2}{c} = 0$ .

### 3.6.2 Special Case # 2: Non-Zero Barycenter Velocity and Invariant Gravitational Potential

rates that are constant and equal except for the unknown influence of absolute velocity. Initially both the absolute velocity of the barycenter and the relation between absolute velocity and clock rate are unknown. As the clocks orbit they communicate time signals for comparison. We shall find both our unknowns from the relation of the clock differences and the orientation in space.

## 4 Velocity Transformation

### 4.1 Relative Velocity of Two Objects

The vector difference of the velocities of two objects in the rest frame gives the relative velocity of the two objects in rest frame metrics. Once we have chosen the frame of reference in which we wish to express the velocity, conversion of relative velocity between rest frame and another frame is simply the application of the distance and angle transformations, time being the same in all frames.

Alternatively, converting coordinates of the two objects at two times and calculating both speed and direction from the converted coordinates effects the same result.

### 4.2 Inverse Frame Velocity

The velocity of the rest frame origin relative to the moving frame origin can be calculated as moving frame distance divided by universal time.

$$v_{\beta,0} = \frac{-\gamma^2\beta ct_0 - 0}{t_0 - 0} = -\gamma^2\beta c \quad (50)$$

FitzGerald relativity does not use the simpler result that comes from using local time instead of universal time.

$$v_\beta = \frac{-\gamma^2 \beta c t_0}{\gamma^2(t_0 - 0) - \gamma^2(0 - 0)}$$

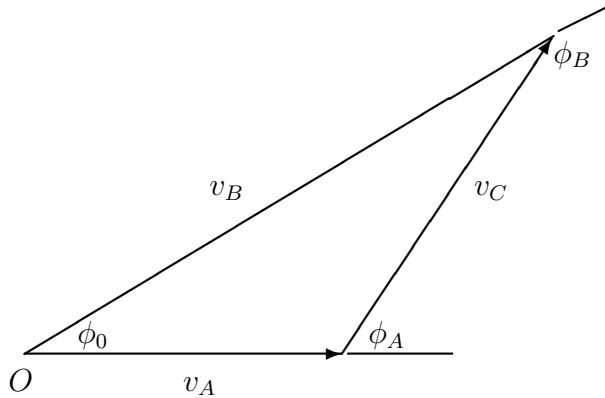
which simplifies to

$$v_\beta = -\beta c \quad (\text{not used})$$

### 4.3 Composition of Velocities

Composition of velocities and relative velocity of two objects are intimately connected. We shall derive composition of velocities by considering relative velocities two moving objects  $A$  and  $B$  with known rest frame velocities  $\vec{v}_A$  and  $\vec{v}_B$  with rest frame angle  $\phi_0$  between them. In figure 2,  $\vec{v}_A + \vec{v}_C = \vec{v}_B$ .

Figure 2



The law of cosines helps us find the rest frame measure of the relative velocity of  $A$  and  $B$ .

$$v_C^2 = v_A^2 + v_B^2 - 2v_A v_B \cos \phi_0 \quad (51)$$

Next, to be able to convert the velocity measure, we must find the angles  $\phi_A$  and  $\phi_B$

$$v_B^2 = v_A^2 + v^2 + 2v_A v_C \cos \phi_A$$

$$\frac{\beta_B^2 c^2 - \beta_A^2 c^2 - v^2}{2\beta_A c v} = \cos \phi_A$$

$$\cos \phi_A = \frac{\beta_B^2 - \beta_A^2 - (\beta_B^2 + \beta_A^2 - 2\beta_B\beta_A \cos \phi_0)}{2\beta_A \sqrt{\beta_B^2 + \beta_A^2 - 2\beta_B\beta_A \cos \phi_0}}$$

$$\cos \phi_A = \frac{-\beta_A + \beta_B \cos \phi_0}{\sqrt{\beta_B^2 + \beta_A^2 - 2\beta_B\beta_A \cos \phi_0}}$$

Similarly

$$\cos \phi_B = \frac{-\beta_B + \beta_A \cos \phi_0}{\sqrt{\beta_B^2 + \beta_A^2 - 2\beta_B\beta_A \cos \phi_0}}$$

Adapting the distance conversion formula, time being the same,

$$v_A = \gamma_A^2 v \sqrt{1 - \beta_A^2 \sin^2 \phi_A} \quad (\text{adapted from (14)})$$

$$v_A = \frac{1}{1 - \beta_A^2} \left( c \sqrt{\beta_B^2 + \beta_A^2 - 2\beta_B\beta_A \cos \phi_0} \right) \sqrt{1 - \beta_A^2 \left( 1 - \left( \frac{-\beta_A + \beta_B \cos \phi_0}{\sqrt{\beta_B^2 + \beta_A^2 - 2\beta_B\beta_A \cos \phi_0}} \right)^2 \right)} \quad (52)$$

For any velocity perpendicular to the x-axis in the moving frame, first with universal time

$$v_{\beta,0,\perp} = \gamma(v_{0,\perp} - \beta c) \quad (53)$$

then with local time

$$v_{\beta,\parallel} = \frac{\gamma^2(v_{0,\parallel} - \beta c)}{1 + \beta^2 \gamma^2 - \frac{v_{0,\parallel}}{\beta c}}$$

$$v_{\beta,\vec{A}\vec{B}} = \frac{\sqrt{(\gamma^2(x_0 - \beta ct_0))^2 + (\gamma y_0)^2}}{t_0 + \beta^2 \gamma^2 \left( t_0 - \frac{x_0}{\beta c} \right)}$$

$$v_{\beta,\vec{A}\vec{B}} = \frac{\sqrt{\gamma^4(x_0 - \beta ct_0)^2 + \gamma^2 y_0^2}}{t_0 + \beta^2 \gamma^2 \left( t_0 - \frac{x_0}{\beta c} \right)}$$

$$v_{\beta,\vec{A}\vec{B}} = \frac{\sqrt{(x_{\beta,B} - x_{\beta,A})^2 + (y_{\beta,B} - y_{\beta,A})^2 + (z_{\beta,B} - z_{\beta,A})^2}}{\gamma \left( t_A - \frac{vx_A}{c^2} \right) - t_{\beta,A}}$$

$$v_A = c \sqrt{\frac{\beta_B^2 + \beta_A^2 - 2\beta_B\beta_A \cos \phi_0}{1 - \beta_A^2} + \frac{(-\beta_A^2 + \beta_A\beta_B \cos \phi_0)^2}{(1 - \beta_A^2)^2}} \quad (54)$$

	Forward	Reverse
$t_B = \gamma \left( t_A - \frac{vx_A}{c^2} \right)$	$t_\beta = t_0 + \beta^2 \gamma^2 \left( t_0 - \frac{x_0}{\beta c} \right)$	$t_0 = t_\beta + \frac{\beta x_\beta}{c}$
$x_B = \gamma(x_A - vt_A)$	$x_\beta = \gamma^2(x_0 - \beta ct_0)$	$x_0 = \frac{x_\beta}{\gamma^2} + \beta ct_0$
$y_B = y_A$	$y_\beta = \gamma y_0$	$y_0 = \frac{y_\beta}{\gamma}$
$z_B = z_A$	$z_\beta = \gamma z_0$	$z_0 = \frac{z_\beta}{\gamma}$

## 5 Length Standardization and the Physics of Length Contraction

Holding to the principle that isotropic light speed is uniquely a rest frame property, defense of that proposition being reserved for section we consider the reliance of international standards on the equivalence of material and interferometric length standards.

From Doiron and Beers, *The Gauge Block Handbook*, Dimensional Metrology Group, Precision Engineering Division, National Institute of Standards and Technology:

Gauge block calibration is one of the oldest high precision calibrations made in dimensional metrology. Since their invention at the turn of the century gauge blocks have been the major source of length standardization for industry. . . .

. . . [We] define the speed of light in vacuum as exactly 299,792,458 m/s, and make length a derived unit. . . . Given the defined speed of light, the wavelength of the light can be calculated, and a meter can be generated by counting wavelengths of the light. Methods for this measurement are discussed in the chapter on interferometry.

There are neither clocks nor multiple reference frames in interferometry. For interferometry and solid gauge blocks to be compatible length standards, the solid gauge block must contract with the contraction, expected by Michelson, of the standing wave pattern of the interferometer light due to the interferometer's motion relative to the rest frame in which light speed is isotropic. Considering that length dimensions of a solid depend on inter-atomic distances that are governed in turn by electromagnetic bonds, this is not surprising; it would be surprising were it otherwise than as FitzGerald conjectured. This now obvious notion did not enter the thinking of others



who, at a time when atomic theory was nascent, struggled to explain the null result of the Michelson Morley experiment. The expectation of a interference fringe shift in that experiment was predicated on the flawed assumption that there was no such variation in the dimensions of solids.

## **6 Falsifications**

### **Part I**

## **Applications**

### **7 The Experiment of Michelson and Morley**

### **8 Maxwell's Electromagnetic Theory**

### **9 An Empirical Method for Determining Absolute Velocity**

### **10 Stellar Aberration**

### **11 The Theory of Mass, Inertia and Gravity**

### **12 Orbital Dynamics**

### **13 Particle Physics**

### **14 The Theory of Atomic and Molecular Spectra**

### **References**